

$$\int_M d\omega = \int_{\partial M} \omega$$



## Metric spaces: $\ell^\infty$

**Question #1** In the metric space  $\ell^\infty$ , i.e., bounded sequences  $(x_n)$  with distance given by the sup-norm,

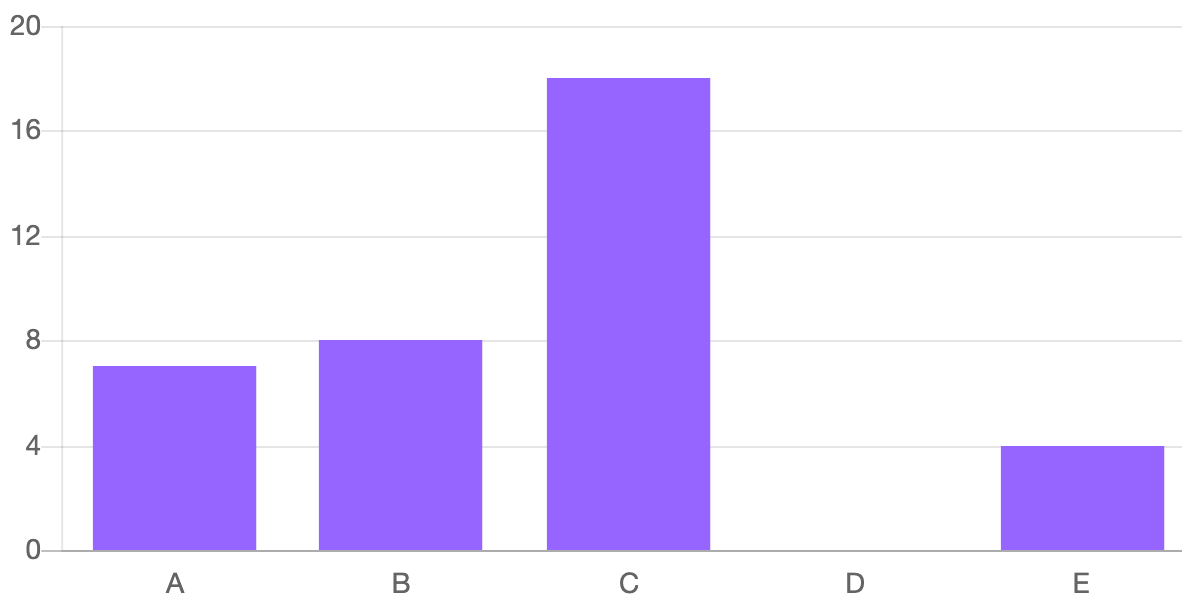
$$d(x, y) = \|x - y\|_\infty = \sup\{|x_n - y_n| : n \in \mathbb{N}\},$$

let

$$E = \{(x_n) \in \ell^\infty : 0 < x_n < 1, \forall n \in \mathbb{N}\}.$$

The interior  $E^\circ$  of the set  $E$  is:

- (A) the empty set  $\emptyset$ ;
- (B) a non-empty subset of  $E$  that is not all of  $E$ ;
- (C) all of  $E$ ;
- (D) all of  $\ell^\infty$ ;
- (E) a black hole.



**Question #2** The closure  $\overline{E}$  of the set  $E$  is:

- (A) the empty set  $\emptyset$ ;
- (B) a non-empty subset of  $E$  that is not all of  $E$ ;
- (C)  $E \cup \{0, 1\}$ ;
- (D)  $\{(x_n) \in \ell^\infty : 0 \leq x_n \leq 1, \forall n \in \mathbb{N}\}$ ;
- (E) a black hole.

