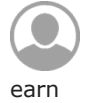


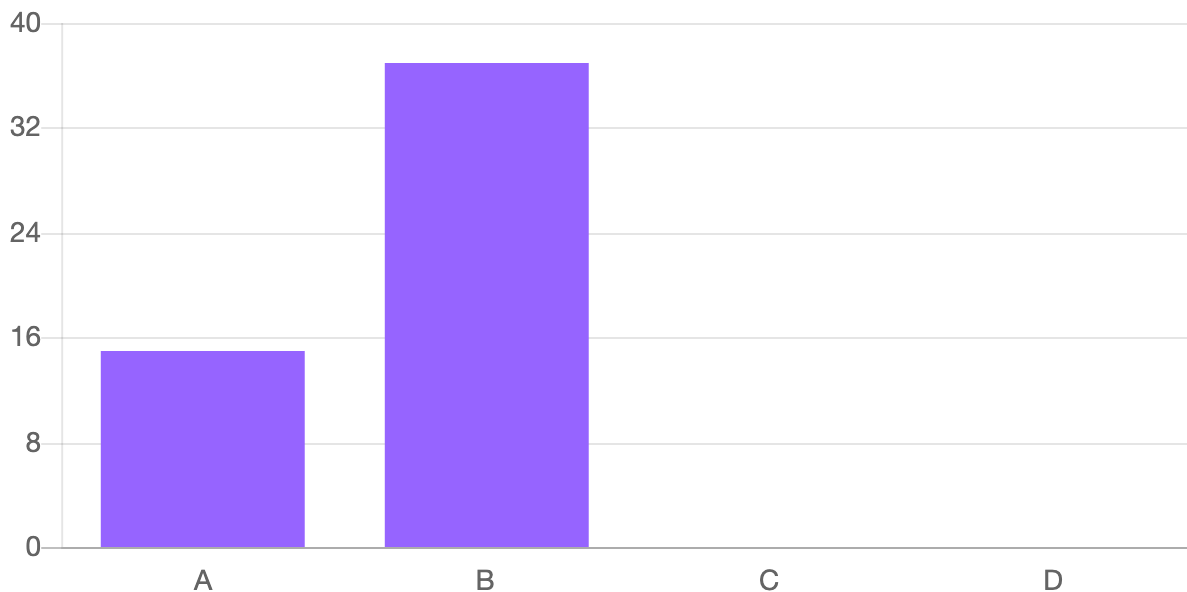
$$\int_M d\omega = \int_{\partial M} \omega$$



Assignment 4: Function sequences

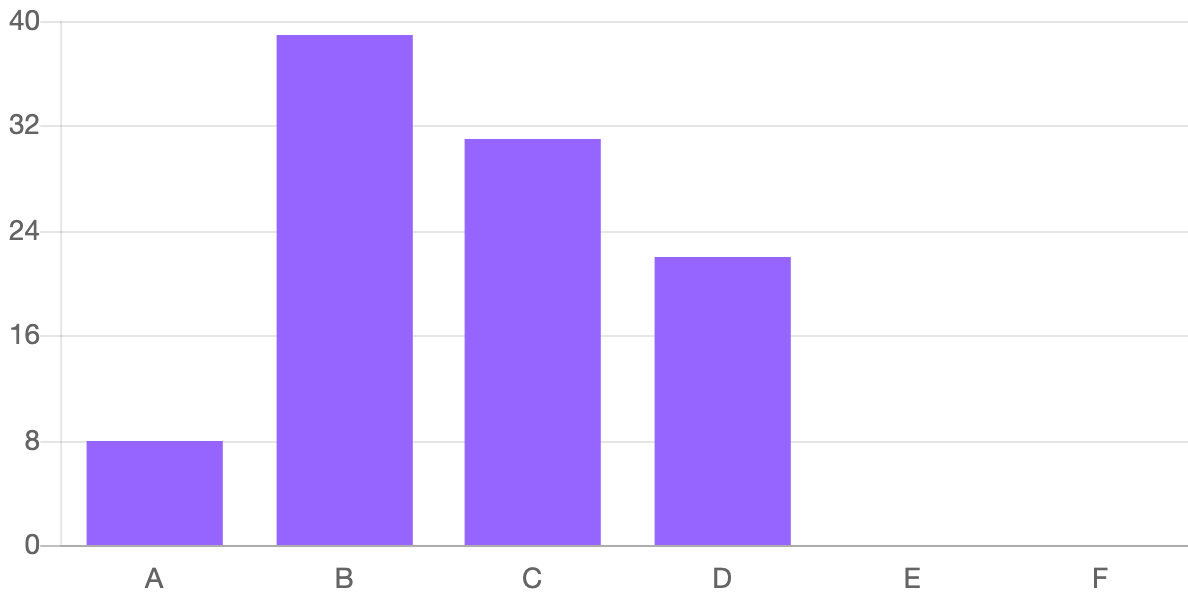
Question #1 Considering $f_n(x) = \sqrt[n]{x}$ on $[0, 1]$, which of the following statements are true?

- (A) $\{f_n\}$ does not converge;
- (B) $\{f_n\}$ converges pointwise;
- (C) $\{f_n\}$ converges uniformly;
- (D) I have not had sufficient time to think about this yet.



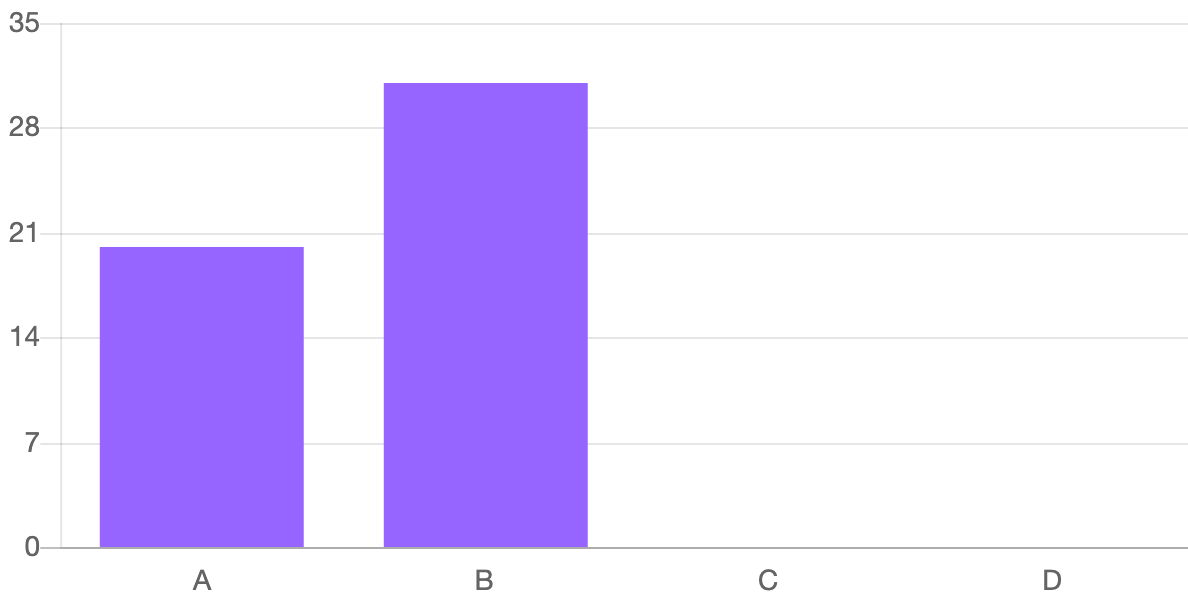
Question #2 Considering $f_n(x) = 0$ if $x \leq n$ and $f_n(x) = x - n$ if $x \geq n$, on $[a, b]$ and on \mathbb{R} , which of the following statements are true?

- (A) $\{f_n\}$ does not converge;
- (B) $\{f_n\}$ converges pointwise on $[a, b]$;
- (C) $\{f_n\}$ converges pointwise on \mathbb{R} ;
- (D) $\{f_n\}$ converges uniformly on $[a, b]$;
- (E) $\{f_n\}$ converges uniformly on \mathbb{R} ;
- (F) I have not had sufficient time to think about this yet.



Question #3 Considering $f_n(x) = \frac{e^x}{x^n}$, on $(1, \infty)$, which of the following statements are true?

- (A) $\{f_n\}$ does not converge;
- (B) $\{f_n\}$ converges pointwise;
- (C) $\{f_n\}$ converges uniformly;
- (D) I have not had sufficient time to think about this yet.



Question #4 Consider the series

$$\sum_{n=1}^{\infty} \frac{x}{n(1+nx^2)}.$$

Which of the following statements are true about this series?

- (A) does not converge for any $x \in \mathbb{R}$;
- (B) converges pointwise on a non-empty set but not on all of \mathbb{R} ;
- (C) converges pointwise on \mathbb{R} ;

(D) converges uniformly on a non-empty set but not on all of \mathbb{R} ;

(E) converges uniformly on \mathbb{R} ;

(F) I have not had sufficient time to think about this yet.

